

Solving Multi-Step Equations 1.2

Multi-Step Equations are equations that take more than one operation to get to the answer.

To solve multi-step equations, work backward by undoing operations.

Remember: Addition/Subtraction are inverse operations and Multiplication/Division are inverse operations.

Example 1: Solve the following equations.

(a). $-12 = 9x - 6x + 15$ * combine like terms

$$\begin{array}{r} -12 = 3x + 15 \\ -15 \quad \downarrow \quad -15 \\ \hline -27 = 3x \end{array}$$

$$\frac{-27}{3} = \frac{3x}{3}$$

$$-9 = x$$

$$\boxed{x = -9}$$

(b). $\frac{h+6}{5} = (2) \cdot 5$

$$\begin{array}{r} h+6 = 10 \\ -6 \quad -6 \\ \hline h = 4 \end{array}$$

$$\boxed{h = 4}$$

Distributive Property: To multiply a sum or difference by a number, multiply each number in the sum or difference by the number outside the parentheses. Then evaluate.

(c). $2(1-x) + 3 = -8$ distribute to ALL terms in the parentheses

$$2 - 2x + 3 = -8$$
 * combine like terms

$$\begin{array}{r} 5 - 2x = -8 \\ -5 \quad \downarrow \quad -5 \\ \hline -2x = -13 \end{array}$$

$$\frac{-2x}{-2} = \frac{-13}{-2}$$

$$\boxed{x = \frac{13}{2}}$$

or 6.5

(d). $\frac{2}{3}(n-6) = -10$

$$\frac{2}{3}n - 4 = -10$$

$$\begin{array}{r} \frac{2}{3}n - 4 = -10 \\ \downarrow +4 \quad +4 \\ \hline \frac{2}{3}n = -6 \end{array}$$

$$\frac{\frac{2}{3}n}{\frac{2}{3}} = \frac{-6}{\frac{2}{3}}$$

$$\frac{2}{3}n = \frac{-6}{\frac{2}{3}}$$

$$n = \frac{-6}{1} \cdot \frac{3}{2}$$

$$\boxed{n = -9}$$



Example 2: Write an equation for each sentence, and then solve the equation.

(a) Fourteen more than a number is equal to twenty-seven.

addition

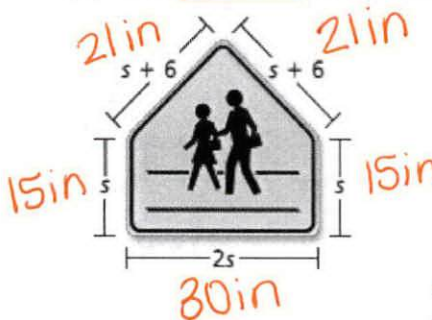
$$\begin{array}{r} 14 + x = 27 \\ -14 \quad -14 \\ \hline x = 13 \end{array}$$

(b) Six times the sum of a number and 15 is -42

$$\begin{array}{r} 6(x + 15) = -42 \\ 6x + 90 = -42 \\ -90 \quad -90 \\ \hline 6x = -132 \\ x = -22 \end{array}$$

Example 3: Write and solve equations which model these real-life situations.

(a) The perimeter of the school crossing sign is 102 inches. What is the length of each side?



P=102

P = sum of all sides

$$102 = (s+6) + (s+6) + s + 2s + s$$

$$102 = s+6 + s+6 + s + 2s + s$$

* combine like terms

$$\begin{array}{r} 102 = 6s + 12 \\ -12 \quad -12 \\ \hline 90 = 6s \\ \frac{90}{6} = \frac{6s}{6} \\ s = 15 \end{array}$$

The length of the sides are 21in, 21in, 15in, 15in, 30in

"per" is the key word for where the variable goes

(b) Your school's drama club charges \$4 per person for admission to a play. The club borrowed \$400 to pay for costumes and props. After paying back the loan, the club had a profit of \$100. How many people attended the play?

- subtraction

$$\begin{array}{r} 100 = 4x - 400 \\ +400 \quad +400 \\ \hline 500 = 4x \\ \frac{500}{4} = \frac{4x}{4} \\ 125 = x \end{array}$$

125 people attended the play

total

Homework: _____

